

## **ESTIMATION OF PARAMETERS CONNECTED ELECTRICAL CONDUCTIVITY OF METALS**

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### **Abstract**

*Different parameters attached to the electrical conductivity of regular metals are evaluated plus are communicated as far as general constants. It happens that they are near those found in metallic copper at room temperature. The way that the acknowledgment of the model happens at room temperature is clarified by utilizing the Landauer's deletion guideline. The arrived at the midpoint of crash time of the electron of conduction is likewise thought as a molecule lifetime. At long last a relationship is built up between the movement of the electron of conduction plus the cosmological consistent issue, where a round surface of span equivalent to the electron mean free way has been thought as a surface skyline for the charge bearers.*

### **Introduction**

Profoundly sanitized water is a terrible electrical transmitter. Be that as it may, the expansion of modest quantities of sodium chloride (NaCl) to this fluid, can expand its electrical conductivity in a considerable manner. At the surrounding temperature (295K), the water's dielectric steady of 80, allows the Na<sup>+</sup> plus Cl<sup>-</sup> particles to move openly through the fluid plus this element can represent the adjustment in its conductive conduct. It appears that the grouping of free charge bearers has the most applicable job in deciding the electrical conductivity of the substances. In any case, what to state about electrical conductivity in metals? Secluded metallic particles have their inward electrons having a place with shut shells plus henceforth firmly bound to their relating nuclear core. Anyway the electrons of the external most shell are feebly attached to its particular nucleus. When masterminded in a precious stone cross section structure, the bond shortcoming of these external electrons is improved because of the communications among neighbor particles of the grid, with the goal that the electrons of conduction are allowed to go through the entire gem. Protection from their movement is because of the warm vibrations (phonons) plus abandons incited by the nearness of polluting influences plus cross section disengagements. In an ideal precious stone at zero total temperature, these free electrons can be portrayed by utilizing the quantum mechanical formalism of the Bloch waves, Kittel (1976), Allen (1979). The grouping of free electrons assumes a significant job in the portrayal of the electrical conductivity in metals.

### Nomenclature

$\Psi$	Field
$E_{av}$	stands for the average energy of the gas
$\alpha$	fine structure constant
$E_M$	Maximum energy
$N$	maximum quantum number
$\ell$	The electron mean free path
$V_F$	The Fermi velocity
$\lambda_C,$	Compton wavelength
$\omega$	Planck length
$\tau$	particle lifetime
$\rho$	resistivity
$F$	Flory-like free energy
$N$	Number of monomers in the chain,
$d$	The space-time dimension
$R_g$	Radius of gyration
$m v_F$	Fermi momentum
$m c.$	Compton momentum
$M_P$	Planck mass,
$L$	Radius of the event horizon of the universe
$\Lambda$	Cosmological constant.
$\Delta F$	Change in free energy

### Evaluation of typical parameters tied to the electrical conductivity of metals

A potential method to assess the centralization of conduction electrons in a run of the mill great metal will be next introduced. An elective structure to assess the Casimir power between two equal uncharged metallic plates isolated by a nearby separation  $d$  was created in reference , Silva (1978). There, we thought about the cutting of a cubic cavity of edge  $d$  in a metallic square. We envisioned that the free electrons in metal as a gas of nonrelativistic particles restricted by the vacuum pressure in the inside of a cubic box of edge equivalent to  $d$ . Then again as was brought up by Jaffe (2005), the Casimir power can be determined without reference to the vacuum variances, plus like other discernible impacts in QED, it disappears as the fine structure steady  $\alpha$  goes to zero. Silva (1978) contemplated a non-relativistic Fermi gas restricted by the vacuum pressure  $B$  plus found the connection

$$B d^3 = \frac{2}{5} E_{av} \quad (1)$$

In the interim it is advantageous to think about that as a proportional method to treat the issue is by considering the electromagnetic cooperation through the reliance of the vitality levels of the framework on the fine structure consistent  $\alpha$ . Perhaps the least complex model which displays vitality levels reliance on the fine structure  $\alpha$  is the Bohr molecule, in particular

$$E_n = \frac{\alpha^2 mc^2}{2n^2} = -\frac{E_1}{n^2} \quad (2)$$

By taking the most extreme involved vitality level equivalent to  $N/2$ , we get the greatest vitality EM of the framework

$$E_M = -\frac{4E_1}{N^2} \quad (3)$$

The average energy could be estimated as

$$E_F = \frac{2}{N} \int_1^N (-) E_1 n^{-2} dn = \frac{2}{N} E_1 \frac{2-N}{N} \quad (4)$$

In the limit, as  $N \gg 1$ , we have

$$E_{av} = -2\frac{E_1}{N} \quad (5)$$

Now let us estimate the vacuum pressure. We have

$$Bd^3 = -\frac{2}{5} \frac{\alpha^2 mc^2}{N} = \frac{2}{5} E_{av} \quad (6)$$

By taking  $P_0 = \frac{amc}{2}$

$\lambda_0 = \frac{h}{P_0} = \frac{2h}{amc}$  it is possible to make the choice

$$N = \frac{d}{\lambda_0} = \frac{amcd}{2h} \quad (7)$$

Inserting equation (7) into equation (6), we obtain

$$B = \frac{8}{5\pi} \frac{\alpha\pi^2 \hbar c}{d^4} \quad (8)$$

In this manner it is seen that by settling on the decision showed by condition (7), the unequivocal reliance of B on the electron mass (m) plus on the most extreme quantum number N has vanished. The elective route utilized so as to treat the Casimir power issue, grant us to compute a run of the mill thickness of charge bearers in great metals. Allow us to compose

$$nd^3 = \frac{4\pi}{3} N^3 3! = 8\pi N^3 \quad (9)$$

In condition (9), the volume of a circle in the N-space is considered, plus the conceivable number of changes among the  $N_x$ ,  $N_y$  plus  $N_z$  quantum numbers. Putting condition (7) into condition (9) we acquire

$$n = \pi \left( \frac{\alpha mc}{h} \right)^3 \quad (10)$$

Numerical assessment of condition (10) gives  $n = 8.56 \times 10^{28} \text{ m}^{-3}$ , which could be contrasted plus  $8.45 \times 10^{28} \text{ m}^{-3}$ , the thickness of charge bearers in metallic copper Kittel (1976), Allen (1979). In the interim the Fermi vitality of metals could be communicated as Kittel (1976), Tiper(1978).

$$E_F = \frac{h^2}{8m} \left( \frac{3n}{\pi} \right)^{\frac{2}{3}} \quad (11)$$

Inserting equation (10) into equation (11), we get

$$E_F = \frac{3^{\frac{2}{3}}}{8} \alpha^2 mc^2 \quad (12)$$

Numerical gauge of condition (12) gives  $E_F = 7.07 \text{ eV}$ , which normally is extremely near the worth found in metallic copper. So as to continue further, let us figure the electrical conductivity of a run of the mill great metal. To do this we initially assume that we have  $n$  dissipates per unit of volume plus by considering a crystal formed cylinder having longitudinal size equivalent to the electron mean free way  $\ell$ , width  $\ell_F$  equivalent to half of the Fermi frequency of the electron, plus thickness  $\ell_C$  equivalent to half of its Compton frequency. In the event that we consider that the electrical conductivity consistently occurs in a system of charge lack of bias, the quantity of dissipates per unit of volume will be equivalent to the number thickness of charge bearers, plus we can compose

$$n \ell_F \ell_C \ell = n \frac{h}{2mv_F} \frac{h}{2mc} v_F \tau \quad (13)$$

In condition (13),  $\ell_C$  represents the frequency of a photon with a force identified with the making of an electron positron pair plus this compares to a base thickness of the crystal, which additionally infers in a greatest  $\tau$ , the normal time between impacts. From condition (13) we acquire the connection

$$n\tau = \frac{m^2 c}{\pi^2 h^2} \quad (14)$$

presently Drude equation for the electrical conductivity is given by Kittel (1976) as

$$\sigma = \frac{e^2 n \tau}{m} \quad (15)$$

Subbing condition (14) into condition (15), we acquire

$$\sigma = \frac{e^2 mc}{\pi^2 h^2} \quad (16)$$

Numerical gauge of the electrical resistivity  $\rho$ , gives  $\rho = 1/\sigma = 1.57 \times 10^{-8} \text{ m}$  which can be contrasted plus the resistivity of the metallic copper estimated at the temperature of 295K, in particular  $\rho_{\text{copper}} = 1.70 \times 10^{-8} \text{ m}$ .

From condition (10) plus condition (14) we additionally get the arrived at the midpoint of time between crashes

$$\tau = \frac{1}{a^3} \frac{4h}{\pi m c^2} \quad (17)$$

Numerical gauge of condition (17) gives  $\tau = 2.65 \times 10^{-14}$ s. This number must be contrasted plus the worth evaluated of  $\tau_{\text{copper}} = 2.5 \times 10^{-14}$ s, for copper at the room temperature as cited by Allen (1978). It is additionally fascinating to compose equations for the Fermi speed  $v_F$  plus the electron mean free way  $\ell$ . We have

$$v_F = \left(\frac{2E_F}{m}\right)^{\frac{1}{2}} = \frac{3^{\frac{3}{2}}}{2} \alpha c, \quad (18)$$

plus

$$\ell = v_F \tau = \frac{3^{\frac{3}{2}}}{\alpha^2} \frac{2h}{\pi m c} \quad (19)$$

These relations for the amounts related to the electrical conduction in run of the mill metals are displayed in table 1, too their individual numerical gauges plus are additionally contrasted plus the comparing ones cited for copper at the room temperature.

### **Realization at the room temperature: a possible explanation**

It is a captivating inquiry why a model portraying the electrical conductivity of a run of the mill great metal just acknowledges itself in copper precious stones at room temperature. The response to this inquiry could be expounded through these reasons. As was brought up by Jacobs (1999), Landauer's deletion rule [8] states that: at whatever point a solitary piece of data is eradicated, the entropy in nature to which the data putting away framework is associated must increment in any event  $k_B \ln 2$ , where  $k_B$  is the Boltzmann's steady;

- A free electron in a metal goes in normal a separation equivalent to its mean free way, with a steady speed  $v_F$ , until to slam into the ionic vibrations (phonons). In the impact procedure, the free electron loses its memory. We imagine that we may partner to the Fermi vitality  $E_F$ , a string of length equivalent to its Fermi frequency, created by unit cells having a length equivalent to the Compton frequency of the electron. Let us to present a semi molecule with a mass-vitality  $\mu c^2$  characterized as

$$\mu c^2 = E_F \frac{v_F}{c} \quad (20)$$

As should be obvious from condition (20), this semi molecule has a mass-vitality equivalent to the Fermi vitality partitioned by the quantity of cells in the string. Characterizing

$$\Delta F = \Delta U - T \Delta S = \frac{1}{2} \mu c^2 - k_B \ln 2 \quad (21)$$

Plus after making the requirement that

$$\Delta F \Big|_{T=T^*} = 0 \quad (22)$$

we obtain the relation

$$E_F^3 = (T^* k_B)^2 2(\ln 2)^2 mc^2 \quad (23)$$

Putting  $E_F = 7.1\text{eV}$  (table 1) plus  $mc^2 = 0.511\text{MeV}$  in equation (23) plus solving for  $k_B T^*$ , we find

$$k_B T^* = 26 \text{ meV} \quad (24)$$

The above number for the trademark temperature  $T^*$  must be contrasted plus  $k_B T_{\text{Room}} = 25\text{meV}$ . In this manner the got outcome for the trademark temperature given by condition (24) appears to sound good to the way that the acknowledgment of the model for the electrical conductivity of good metals to occur for copper gems at the room temperature.

### Three trademark lengths plus the develop of a polymer chain

In a paper managing the cosmological consistent issue, Silva (20086), the time development of the universe world line was contrasted plus the developing of a polymer chain by utilizing a Flory-like free vitality. It is conceivable to think the electron mean free way as the length of a polymer chain, made by monomers out of size equivalent to the Compton frequency of electron. Inside this similarity, the span of gyration of the chain is related to the Fermi frequency of electron. We consider as in the de Gennes inference (1979) two commitments for the Flory's free vitality. The principal term which goes relative to  $N^2/R^d$   $N^2 R^d$ , compares to an unpleasant like monomer-monomer interaction. A second term which originates from an entropic commitment, in particular a logarithm of a Gaussian dissemination (a mark of an irregular walk process) goes as goes as  $\frac{R^2}{(N\lambda_C)^2}$ . We write

$$F = \frac{N^2 \lambda_c^d}{R^d} + \frac{R^2}{N\lambda_c^2} \quad (25)$$

. Setting  $\ell = N\lambda_C$  plus limiting condition (25) comparative with  $R$ , we get for the span of gyration  $R_g$ , the Connection

$$R_g = \ell^{\frac{3}{2+d}} \lambda_c^{\frac{d-1}{2+d}} \quad (26)$$

We identify  $R_g$  ( $d = 4$ ) with the Fermi length of the electron  $\lambda_F$  We have

$$\lambda_F = (\ell \lambda_c)^{\frac{1}{2}} \quad (27)$$

We see that condition (27), relating the three attributes lengths of the issue, concurs with the upper bound to the electron mean free way found in Silva (2006). It would be ideal if you see condition (21) of the referred to

reference. It is worth to see that the understanding between the two figurings happens exactly when the sweep of gyration is assessed in the space-time measurement  $d = 4$ .

### High temperature behaviour of the collision time

It is fascinating to assess a connection communicating the high temperature conduct of the crash time showing up in the Drude equation for the electrical conductivity. By considering a thick power which relies directly upon the speed, the force scattered by this power can be composed as

$$\frac{dE}{dt} = -F_{viscous} v = -\frac{1}{\tau} p v \quad (28)$$

The force dispersed by this gooey power following up on the charge bearer will show up as an expanding in the inward vitality of the cross section plus we compose

$$\frac{dU}{dt} = -\frac{dE}{dt} = \frac{1}{\tau} \rho v \quad (29)$$

By taking

$$\rho = \frac{\hbar}{2R} \text{ plus } v dt = dR \quad (30)$$

where the first relation in equation (30) comes from the uncertainty principle, we get

$$dU = \frac{\hbar}{2\tau} \frac{dR}{R} \quad (31)$$

Performing the integration of equation (31) between the limits  $R_0 = \frac{\hbar}{mc}$  plus

$$R_1 = \frac{\hbar}{mv_1} \text{ we obtain}$$

$$\Delta U = \frac{\hbar}{2\tau} \ln \frac{c}{v_F} \quad (32)$$

Now, let us consider an entropy variation given by

$$\Delta S = k_B \ln 2^D = D k_B \ln 2. \quad (33)$$

In condition (33), we have composed an entropy variety like that considered in applying the Landauer's deletion standard (1961), however here putting  $D = 4$ , by considering the four elements of the space-time. Taking the extremum of the free vitality, specifically composing

$$\Delta F = \Delta U - T \Delta S = 0 \quad (34)$$

plus solving for  $\tau$ , we have

$$\tau = \frac{\hbar}{8k_B T} \ln \frac{c}{v_F} \quad (35)$$

In the case of copper  $v_F = 1.57 \times 10^6 \text{ m s}^{-1}$  at the room temperature ( $T = 300\text{K}$ ), we find

$$\tau_{cooper}(300k) = 2.4 \times 10^{-14} \text{ s} \quad (36)$$

As appeared in table 1, the aftereffect of condition (36) is near the room temperature mean crash time of the electrons of conduction in copper, as cited in the writing.

### Average collision time as a particle lifetime

There are two attributes straight momenta that we can partner to the free electrons liable for the electrical conductivity in great metals. They are: the Fermi energy  $mv_F$  plus the Compton force  $mc$ . By considering that the free electron has a fermionic character, we will compose a non-straight Dirac-like condition portraying the "movement" of this molecule. We have

$$\frac{\partial \Psi}{\partial x} = \frac{1}{c} \frac{\partial \Psi}{\partial t} = \frac{mv_F}{\hbar} \Psi - \frac{mc}{\hbar} \Psi \quad | \Psi * \Psi | \Psi. \quad (37)$$

Condition (37) contains just first request subsidiaries of the field  $\Psi$ . Other than this, the field  $\Psi$ , has not a spinorial character. Making the different sides of condition (37) equivalent to zero plus explaining for  $|\Psi * \Psi|$  we get

$$|\Psi * \Psi| = \frac{v_F}{c} = \frac{3^3}{2} \alpha. \quad (38)$$

In acquiring condition (38), we additionally utilized the outcome for  $v_F$  appeared in table 1. Then again in the impact procedure, the free electron misfortune its memory.

This component appears to be like the destruction of a molecule antiparticle pair, every one of mass-vitality equivalent to  $E_F$ . Placing this thing in a type of the vulnerability rule yields.

$$2 E_F \Delta t = \frac{h}{2} \text{ or } \frac{hv}{2} = 2E_F \quad (39)$$

Solving equation (39) for  $v$ , we get

$$v = \frac{1}{\Delta t} = 4 \frac{E_F}{h} = \frac{3^3}{2h} \alpha^2 mc^2 \quad (40)$$

By joining the consequences of condition (38) plus equation(40) we acquire the line width  $\Gamma$  attached to the "molecule" rot

$$\Gamma = v \quad | \Psi * \Psi | = \frac{3}{4h} \alpha^3 mc^2 \quad (41)$$

Finally the "particle" lifetime  $\tau$  is given by

$$\tau = \frac{1}{\Gamma} = \frac{4h}{mc^2 3\alpha^3}$$

(42)Contrasting  $\tau$  giving by condition (42) with the time between impacts appeared in table

Table 1: Equations identified with the electrical conductivity of ordinary metals, as far as all inclusive constants (this work). Numerical assessments of them are contrasted plus those cited for Copper at room temperature.



Formula	Numerical estimates	Copper at room temperatures
$n = \pi \left( \frac{\alpha mc}{h} \right)^3$	$8.56 \times 10^{28} \text{ m}^{-3}$	$8.45 \times 10^{28} \text{ m}^{-3}$ [1,2]
$E_F = \frac{2}{8} \alpha^2 mc^2$	7.07 eV	7.0 eV
$\rho = \frac{1}{\sigma} = \frac{\pi^2 \hbar^2}{c^2 mc}$	$1.57 \times 10^{-8} \Omega \text{ m}$	$1.70 \times 10^{-8} \Omega \text{ m}$
$\tau = \frac{1}{\alpha^2} \frac{4h}{\pi mc^2}$	$2.65 \times 10^{-14} \text{ s}$	$2.5 \times 10^{-14} \text{ s}$
$v_F = \frac{1}{2} \alpha c$	$1.6 \times 10^6 \text{ m s}^{-1}$	$1.6 \times 10^6 \text{ m s}^{-1}$
$\ell = \frac{1}{\pi mc \alpha^2}$	419 Å	400 Å

### Analogy with the cosmological constant problem

Right now expect, for straightforwardness, that  $\hbar = c = k_B = 1$ . One worth point we can consider now is the relationship that can be made with the cosmological consistent issue. Hsu plus Zee (1993) have proposed a successful activity  $A_{eff}$  as a way to manage the cosmological steady issue. They composed

$$A_{eff} = - \left( \Lambda L^4 + \frac{M_P^4}{\Lambda} \right) + \text{independent of } \Lambda \text{- terms,} \quad (43)$$

Taking the extremum of this action they got

$$\Lambda = \left( \frac{M_P}{L} \right)^2 \quad (44)$$

We could think  $A_{eff}$  above as a four-dimensional portrayal of a sort of free vitality, where the primary term assumes the job of the interior vitality plus the subsequent one is identified with the entropy  $S$ . The supreme temperature is taken to be equivalent to one. We recommend that

$$\Omega \sim \exp\left(\frac{M_P^4}{\Lambda}\right) \quad (45)$$

With

$$S = \ln \Omega \quad (46)$$

Susskind (2006), recommended that the universe can be considered as a dark opening with its entropy being assessed by checking the quantity of cells contained in the region of its occasion skyline (the holographic guideline), specifically

$$S_{universe} \sim \left(\frac{L}{L_p}\right)^2 = L^2 M_p^2 \quad (47)$$

By thinking about the two comparable methods for the entropy assessment, from condition (46) plus condition (47) relations, we can compose

$$L^2 M_p^2 = \frac{M_p^4}{\Lambda} \quad (48)$$

which repeats the aftereffects of Hsu plus Zee (1993), if you don't mind see condition (44). Going to the issue of the electrical conductivity in great metals, let us consider for example in a copper precious stone an electron of the conduction band which just endured an impact. Without an outside electric field, all the bearings in the space have equivalent likelihood to be picked in a beginning new free flight. Subsequently on the off chance that we take a circle focused at where the electron has been dissipated, with a span equivalent to the electron mean free way, the outside of this circle might be considered as an occasion skyline for the marvels. Any electron beginning from this inside will be on normal dissipated when striking the occasion skyline, loosing the memory of its past free flight. Other than this, all the cross section destinations of the metallic gem are treated on equivalent balance, because of the translational balance of the framework. In view of the past conversation plus enlivened on the dark gap material science, let us to characterize the entropy related on the occasion skyline for the electron of conduction in metals.

$$S_{metal} = \pi \left(\frac{\ell}{w}\right)^2 \quad (49)$$

It is conceivable to compose an activity comparable to that of Hsu plus Zee (1993), so as to depict the electrical conductivity in metals. We have

$$A_{Metal} \sim \left(\Lambda_M \ell^4 + \frac{1}{\Lambda w^4}\right) \quad (50)$$

Making the fairness between the two different ways of composing the entropy, to be specific rising to the entropy of a surface skyline of sweep  $\ell$  plus ultra-violet cutoff  $w$  with the last term of condition (50), we get

$$\pi \left[\left(\frac{1}{w}\right)\right]^2 = 1/(\Lambda_M w^4) \quad (51)$$

which prompts

$$\Lambda_M^{-1/2} = \pi^{1/4} \left[\left(\frac{1}{w}\right)\right]^{1/2} \quad (52)$$

Upon to recognize  $\Lambda_M^{-1/2}$  with the Fermi frequency of the electron  $\lambda_F$  plus  $w$  with its Compton frequency  $\lambda_C$ , we get

$$\lambda_F = \pi^{1/4} \left[ (\lambda_C) \right]^{1/2} \quad (53) \quad \pi \left( \frac{\ell}{w} \right)^2 = \frac{1}{\Lambda_M w^4}$$

(51)

which leads to

$$\Lambda_M^{-1/2} = \pi^{1/4} (\ell w)^{1/2} \quad (52)$$

Upon to identify  $\Lambda_M^{-1/2}$  with the Fermi wavelength of the electron  $\lambda_F$  plus  $w$  with its Compton wavelength  $\lambda_C$ , we obtain

$$\lambda_F = \pi^{1/4} (\ell \lambda_C)^{1/2} \quad (53)$$

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